

Exercises to the lecture  
Complexity Theory  
Sheet 5

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Delivery until 17.01.2022 at 15:00

**Exercise 5.1** (Parameterized SAT)

Consider the following parameterized problem:

*Boolean Satisfiability* (SAT)**Input:** A Boolean formula  $\varphi(x_1, \dots, x_k)$ .**Parameter:**  $k \in \mathbb{N}$ .**Question:** Is there a satisfying assignment for  $\varphi$ ?

Construct a search tree for SAT and show that the problem is FPT.

**Exercise 5.2** (Unions of cliques)

A *clique* is a graph  $K = (V, E)$  such that for all  $u, v \in V$  we have  $uv \in E$ . This means that any pair of vertices has a connecting edge. The following problem asks how *far away* a given graph is from being a union of cliques.

*Cluster Editing* (CLUSTER)**Input:** A graph  $G = (V, E)$  and a  $k \in \mathbb{N}$ .**Parameter:**  $k \in \mathbb{N}$ .**Question:** Is it possible to add or remove at most  $k$  edges to/from  $E$  such that the resulting graph is a disjoint union of cliques?

- Show that a graph  $G$  consists of disjoint cliques if and only if there are no three distinct vertices  $u, v, w \in V$  with  $uv, vw \in E$  and  $uw \notin E$ .
- Prove that CLUSTER is FPT.

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